# $\mathrm{PbWO}_{4}$-III (A High-Pressure Form) 

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Abstract. $\mathrm{PbWO}_{4}$-III, monoclinic, $P 2_{1} / n, a=12.709$ (5), $b=7.048$ (3), $\quad c=7.348$ (3) $\AA, \quad \beta=90.57$ (4) ${ }^{\circ}, \quad Z=8$, $D_{c}=9.19 \mathrm{~g} \mathrm{~cm}^{-3}$. Crystals were prepared under high pressure at high temperature in the presence of water. $\mathrm{PbWO}_{4}$-III is formally isomorphous with $\mathrm{BaWO}_{4}-\mathrm{II}$, but the coordination number of both sets of Pb atoms is eight.

Introduction. $\mathrm{PbWO}_{4}$ occurs in nature as tetragonal stolzite ( $\mathrm{PbWO}_{4}-\mathrm{I}$, scheelite-type) and monoclinic raspite $\left(\mathrm{PbWO}_{4}-\mathrm{II}\right.$, unique structure, not wolframitetype). $\mathrm{PbWO}_{4}-\mathrm{II}$ is $1 \cdot 3 \%$ less dense than $\mathrm{PbWO}_{4}-\mathrm{I}$ (Shaw \& Claringbull, 1955), and has not yet been prepared synthetically. $\mathrm{PbWO}_{4}$-III exists above the pressure $P(\mathrm{kbar})=0.7+0.039 T\left({ }^{\circ} \mathrm{C}\right)\left(T=350-650^{\circ} \mathrm{C}\right)$, and is quenchable to normal pressure (Chang, 1971).

Single crystals of $\mathrm{PbWO}_{4}$-III were prepared by sealing precipitated $\mathrm{PbWO}_{4}-\mathrm{I}$ with a small amount of distilled water in a thin-walled Pt capsule, treating this for 4 h in a piston-cylinder device (Kennedy \& LaMori, 1961) at $500^{\circ} \mathrm{C}, 32 \mathrm{kbar}$, and cooling slowly before release of pressure.

Intensities were collected on a Philips PW1100 four-circle diffractometer in the $\omega-2 \theta$ mode with graphite-monochromated Mo $K \alpha$ radiation. A roughly spherical crystal with radius 0.1 mm was used. Data
were collected to the limit of the Cu sphere $(\theta=3-$ $27.4^{\circ}$ ) at a scan rate of $0.04^{\circ} \mathrm{s}^{-1}$ and a constant scan width of $1 \cdot 4^{\circ}$. The background was counted for half the total scanning time on each side of the reflexion. Of the 1501 independent reflexions measured, 399 were considered unobserved with $I<2 \sigma(I)$. The systematic absences were $h 0 l, h+l=2 n+1$, and $0 k 0, k=2 n+1$, indicating the space group $P 2_{1} / n$. The large $\mu R$ of 8.73 necessitated absorption corrections, and corrections for a spherical crystal were applied.
Since the cell dimensions and space group indicated that $\mathrm{PbWO}_{4}-\mathrm{III}$ is probably isomorphous with the high-pressure phase $\mathrm{BaWO}_{4}$-II (Kawada, Kato \& Fujita, 1974), the fractional coordinates found there were used as the starting point for full-matrix leastsquares refinement. The temperature factors of the O atoms were refined isotropically. The function minimized was $\sum \omega(\Delta F)^{2}$ with $1 / \sigma_{F}^{2}$ weights. $R=\sum \Delta F / \sum F_{o}$ and $R_{w}=\left[\Sigma \omega(\Delta F)^{2} / \Sigma \omega F\right]^{1 / 2}$ converged to final values of 0.056 and 0.066 , respectively. The atomic parameters are listed in Table 1.*

* A list of structure factors has been deposited with the British Library Lending Division as Supplementary Publication No. SUP 31472 (11 pp., 1 microfiche). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 13 White Friars, Chester CHI 1NZ, England.


Fig. 1. A stereo view (Johnson, 1971) of $\mathrm{PbWO}_{4}$-III down $b$. $a$ is horizontal and $c$ vertical, down. Pb and W atoms are represented by the largest and smallest circles, respectively.

Table 1. Fractional coordinates ( $\times 10^{4}$ ) and thermal parameters $\left(\AA^{2} \times 10^{4}\right)$ with e.s.d.'s Anisotropic thermal parameters are of the form $T=\exp \left[-2 \pi^{2}\left(a^{* 2} h^{2} U_{11}+\ldots 2 b^{*} c^{*} k l U_{23}\right)\right]$.

|  | $x$ | $y$ | $z$ | $U_{11}$ | $U_{22}$ | $U_{33}$ | $U_{12}$ | $U_{13}$ | $U_{23}$ |
| ---: | ---: | :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | $x b(1)$ | $1486(1)$ | $6887(2)$ | $1568(2)$ | $146(7)$ | $152(8)$ | $195(7)$ | $14(6)$ | $30(5)$ |
| $\mathrm{Pb}(2)$ | $1445(1)$ | $9410(2)$ | $6316(2)$ | $165(7)$ | $191(8)$ | $148(6)$ | $-23(6)$ | $41(5)$ | $5(6)$ |
| $\mathrm{W}(1)$ | $840(1)$ | $1642(2)$ | $876(2)$ | $77(7)$ | $67(7)$ | $53(6)$ | $-4(5)$ | $28(4)$ | $-4(5)$ |
| $\mathrm{W}(2)$ | $894(1)$ | $4520(2)$ | $6499(2)$ | $64(6)$ | $70(7)$ | $59(6)$ | $2(5)$ | $29(4)$ | $11(5)$ |

Table 1 (cont.)

|  |  | $y$ | $z$ | $U$ |
| :--- | ---: | :---: | :---: | ---: |
|  |  | $y$ | $z$ | $U$ |
| $\mathrm{O}(1)$ | $958(22)$ | $175(43)$ | $2849(37)$ | $157(56)$ |
| $\mathrm{O}(2)$ | $1837(20)$ | $5856(40)$ | $7837(34)$ | $116(51)$ |
| $\mathrm{O}(3)$ | $559(19)$ | $6450(37)$ | $4755(31)$ | $63(46)$ |
| $\mathrm{O}(4)$ | $2159(21)$ | $2556(42)$ | $554(38)$ | $155(56)$ |
| $\mathrm{O}(5)$ | $522(21)$ | $2726(42)$ | $8267(37)$ | $145(53)$ |
| $\mathrm{O}(6)$ | $1754(20)$ | $3099(40)$ | $5238(34)$ | $116(51)$ |
| $\mathrm{O}(7)$ | $261(20)$ | $3779(40)$ | $186(35)$ | $121(52)$ |
| $\mathrm{O}(8)$ | $789(19)$ | $9198(40)$ | $9416(34)$ | $111(50)$ |

All calculations were done with the X-RAY system of crystallographic programs (Stewart, Kruger, Ammon, Dickinson \& Hall, 1972). The scattering factors were taken from Cromer \& Mann (1968). Cell dimensions were obtained from a least-squares fit of highangle peaks in the powder pattern.

Discussion. $\mathrm{PbWO}_{4}-\mathrm{III}$ is isomorphous with $\mathrm{BaWO}_{4}$-II. The structure contains densely packed two-dimensional networks of slightly distorted $\mathrm{WO}_{6}$ octahedra linked by Pb atoms. Fig. 1 illustrates two of these layers and their positions relative to the unit cell.

The bond lengths and angles are listed in Tables 2 and 4. The only significant differences between the structures of $\mathrm{BaWO}_{4}-\mathrm{II}$ and $\mathrm{PbWO}_{4}$-III are in the coordination around the Pb atoms. The average $\mathrm{Pb}-\mathrm{O}$ distance is $2.67 \AA$ for both sets of Pb atoms, while the average $\mathrm{Ba}-\mathrm{O}$ distances are 2.83 and $2.76 \AA$ for $\mathrm{Ba}(1)$ and $\mathrm{Ba}(2)$, respectively. $\mathrm{Pb}(1)$ is surrounded by eight O atoms between 2.43 and $2.88 \AA$ with the next nearest, $\mathrm{O}(4)$, at $3.28 \AA$, whereas $\mathrm{Ba}(1)$ has nine O atoms, including $\mathrm{O}(4)$, surrounding it at distances between 2.72 and $3.05 \AA$ with the next nearest at $3.20 \AA$. The comparison in Table 4 between the bond lengths in $\mathrm{BaWO}_{4}-\mathrm{II}$ and $\mathrm{PbWO}_{4}$-III clearly shows that the environments of the Ba and Pb atoms differ significantly. The lower effective coordination about $\mathrm{Pb}(1)$ compared to $\mathrm{Ba}(1)$ is reflected in the density. $\mathrm{BaWO}_{4}$-II is $12 \cdot 7 \%$ denser than scheelite-type $\mathrm{BaWO}_{4}-\mathrm{I}$, whereas $\mathrm{PbWO}_{4}$-III is only $8.7 \%$ denser than scheelite-type $\mathrm{PbWO}_{4}-\mathrm{I}$.

Table 2. Interatomic distances ( $\AA$ ) around W atoms W-O

|  | W(1) |  | W(2) |
| :---: | :---: | :---: | :---: |
| $\mathrm{O}(1)$ | 1.79 (3) | $\mathrm{O}(2)$ | $1 \cdot 81$ (3) |
| $\mathrm{O}(4)$ | 1.81 (3) | $\mathrm{O}(3)$ | 1.91 (3) |
| $\mathrm{O}(7)$ | 1.83 (3) | O(5) | $1 \cdot 88$ (3) |
| $\mathrm{O}\left(5^{\text {i }}\right.$ ) | $2 \cdot 10$ (3) | O (6) | 1.76 (3) |
| $\mathrm{O}\left(8^{\text {ii) }}\right.$ ) | 2.03 (3) | $\mathrm{O}\left(3^{\text {iii }}\right.$ ) | $2 \cdot 17$ (3) |
| $\mathrm{O}\left(8^{\text {iii }}\right)$ | $2 \cdot 16$ (3) | $\mathrm{O}\left(7^{\mathrm{iii}}\right)$ | 2.26 (3) |
| Average | 1.95 | Average | 1.97 |
| $\mathrm{O}-\mathrm{O}$ |  |  |  |
| Min. | 2.47 (3) | Min. | 2.51 |
| Max. | 3.06 | Max. | 2.96 |
| Average | $2 \cdot 75$ | Average | 2.75 |

[^0]Table 3. Bond angles $\left({ }^{\circ}\right)$ around W atoms (all angles have an e.s.d. of $\pm 1^{\circ}$ )

| Around $\mathrm{W}(1)$ atom |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
|  | $\mathrm{O}(4)$ | $\mathrm{O}(7)$ | $\mathrm{O}\left(5^{\mathrm{i}}\right)$ | $\mathrm{O}\left(8^{\mathrm{ii}}\right)$ | $\mathrm{O}\left(8^{\mathrm{ili}}\right)$ |
| $\mathrm{O}(1)$ | 104 | 101 | 165 | 87 | 90 |
| $\mathrm{O}(4)$ |  | 98 | 85 | 105 | 166 |
| $\mathrm{O}(7)$ |  |  | 89 | 154 | 83 |
| $\mathrm{O}\left(5^{\mathrm{i}}\right)$ |  |  |  | 80 | 80 |
| $\mathrm{O}\left(8^{\mathrm{i}}\right)$ |  |  |  |  | 72 |


| Around $\mathrm{W}(2)$ atom |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{O}(3)$ | $\mathrm{O}(5)$ | $\mathrm{O}(6)$ | $\mathrm{O}\left(3^{\mathrm{iii}}\right)$ | $\mathrm{O}\left(7^{\text {ili }}\right)$ |
| $\mathrm{O}(2)$ | 98 | 98 | 100 | 162 | 82 |
| $\mathrm{O}(3)$ |  | 152 | 101 | 76 | 81 |
| $\mathrm{O}(5)$ |  |  | 98 | 82 | 80 |
| $\mathrm{O}(6)$ |  |  | 97 | 177 |  |
| $\mathrm{O}\left(3^{\mathrm{iii}}\right)$ |  |  |  |  | 81 |

Table 4. Interatomic distances $(\AA)$ between Pb and O atoms in $\mathrm{PbWO}_{4}-\mathrm{III}$, compared to the corresponding $\mathrm{Ba}-\mathrm{O}$ distances in $\mathrm{BaWO}_{4}-\mathrm{II}$
$\mathrm{Pb}-\mathrm{O}$ and $\mathrm{Ba}-\mathrm{O}$

|  | $\mathrm{Pb}(1)$ | $\mathrm{Ba}(1)$ |  | $\mathrm{Pb}(2)$ | $\mathrm{Ba}(2)$ |
| :--- | :---: | :--- | :--- | :---: | :---: |
| $\mathrm{O}\left(1^{\mathrm{i}}\right)$ | $2.59(3)$ | 2.95 | $\mathrm{O}\left(1^{\mathrm{i}}\right)$ | $2.67(3)$ | 2.67 |
| $\mathrm{O}\left(2^{\mathrm{if}}\right)$ | $2.88(3)$ | 2.76 | $\mathrm{O}(2)$ | $2.79(3)$ | 2.79 |
| $\mathrm{O}(3)$ | $2.65(3)$ | 2.81 | $\mathrm{O}\left(2^{\text {v }}\right)$ | $2.49(3)$ | 2.64 |
| $\mathrm{O}(4)$ | $[3.28(3)]^{*}$ | 3.05 | $\mathrm{O}(3)$ | $2.63(3)$ | 2.74 |
| $\mathrm{O}\left(4^{\text {iii }}\right)$ | $2.76(3)$ | 2.76 | $\mathrm{O}\left(4^{\text {iii }}\right)$ | $2.61(3)$ | 2.83 |
| $\mathrm{O}\left(5^{\mathrm{iv}}\right)$ | $2.57(3)$ | 2.80 | $\mathrm{O}\left(5^{\mathrm{i}}\right)$ | $2.99(3)$ | 3.05 |
| $\mathrm{O}\left(6^{\text {iii }}\right)$ | $2.75(3)$ | 2.91 | $\mathrm{O}\left(6^{\mathrm{i}}\right)$ | $2.75(3)$ | 2.85 |
| $\mathrm{O}(7)$ | $2.70(3)$ | 2.75 | $\mathrm{O}(8)$ | $2.44(3)$ | 2.52 |
| $\mathrm{O}\left(8^{\text {ii }}\right)$ | $2.43(3)$ | 2.72 | Average | 2.67 | 2.76 |
| Average | 2.67 | 2.83 |  |  |  |

Symmetry code: i $x, 1+y, z$; ii $x, y,-1+z$; iii $\frac{1}{2}-x, \frac{1}{2}+y, \frac{1}{2}-z$; iv $-x, 1-y, 1-z ; \vee \frac{1}{2}-x, \frac{1}{2}+y, \frac{3}{2}-z$.

* Not included in average value.

Phases similar to $\mathrm{BaWO}_{4}-\mathrm{II}$ and $\mathrm{PbWO}_{4}-\mathrm{III}$ may possibly occur at high pressures also in the corresponding molybdates. No $\mathrm{ABO}_{4}$-type phases are known as yet that are more densely packed than $\mathrm{BaWO}_{4}$-II.

## References

Chang, L. L. Y. (1971). J. Amer. Ceram. Soc. 54, 357-358.
Cromer, D. T. \& Mann, J. B. (1968). Acta Cryst. A24, 321-324.
Johnson, C. K. (1971). ORTEP-II. Oak Ridge National Laboratory Report ORNL-3794.
Kawada, I., Kato, K. \& Fuitra, T. (1974). Acta Cryst. B30, 2069-2071.
Kennedy, G. C. \& Lamori, P. N. (1961). In Progress in very High Pressure Research. Edited by P. F. Bundy, W. R. Hibbard \& H. M. Strong. New York: John Wiley.
Shaw, R. \& Claringbull, G. F. (1955). Amer. Min. 40, 933.
Stewart, J. M., Kruger, G. J., Ammon, H. L., Dickinson, C. \& Hall, S. R. (1972). The X-RAY system, version of June 1972. Tech. Rep. TR-192, Computer Science Center, Univ. of Maryland, College Park, Maryland.


[^0]:    Symmetry code: i $x, y,-1+z$; ii $x,-1+y,-1+z$; iii $-x, 1-y, 1-z$.

